

Yices – A SMT solver

Introduction
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SAT solver

- (Boolean) SAT(satisfiability) solver
 - A CASE tool which finds set of values satisfy logical formula.
 - Usually embedded other CASE tool.

- Basic SAT solver
 - $A \& B = \text{true} \rightarrow \text{SAT solver} \rightarrow \text{unsat}$
 - $A \& B \& (A = \text{true}) \& (B = \text{true}) = \text{true} \rightarrow \text{SAT solver} \rightarrow \text{sat}$

- General SAT solver
 - $A \& B = \text{true} \rightarrow \text{SAT solver} \rightarrow A = \text{true}, B = \text{true}$
 - Only one set of values

Satisfiability Modulo Theories(SMT)

- SMT is a problem of determining satisfiability of formulas modulo background theories.
- Examples of background theories:
 - Linear arithmetic: $x + 1 \leq y$
 - Arrays: $a[i := v_i][j] = v_2$
 - Uninterpreted function: $f(f(fx))) = x$
 - Datatypes: $car(cons(v_1, v_3)) = v_2$
 - Bitvectors: $concat(bv_1, bv_2) = bv_3$

User interface

- No GUIs.
- Input file: *.ys
- User friendly mode (shell)
 - ./yices -i
- Usage (cygwin)
 - ./yices -[options] *.ys

Types

- Basic types
 - int
 - bool
 - nat (natural numbers)
 - real
 - bit-vector (user defined size)
 - User defined types

- Types
 - Function, record(stack), tuple, constant

- Form
 - define [name]::[type]
 - e. g.) basic: (define i::int)
 - e. g.) functions: (define f::(-> int int))
 - tuple: (tuple [type_1] ... [type_n])
 - e. g.) (define t1::(tuple int bool int))

Expressions

- Boolean operations
 - Form: (and [expr_1] ... [expr_n]) (or [expr_1] ... [expr_n]) (not [expr]) (\Rightarrow [expr_1] [expr_2])
 - not expr_i: !expr_i
 - or, and expr_i expr_j: (or, and expr_i expr_j)

- Equality and disequality
 - Form: (= [expr_1] [expr_2]) (\neq [expr_1] [expr_2])

- If-then-else
- Let (similar with #define in C)
- Quantifier
- Arithmetic(linear): +, -, *, /, <, >, <=, >=

Assert

- Assert: gets only trivial inconsistencies
 - Form: `assert [expr]`
- Extended Assert: gets unsatisfiable cores;

```
(define x::bool)
(define y::bool)
(assert (not x))
(assert (not y))
(assert+ (or x y))
=> 1
(check)
=> unsat
(retract 1)
(check)
=> sat
```



id of assert+

```
(set-evidence! true)
(set-verbosity! 2)
(define x::bool)
(define y::bool)
(define z::bool)
(define w::bool)

(assert+ (/= x y))
=> id: 1
(assert+ (/= y z))
=> id: 2
(assert+ (or w x y))
=> id: 3
(assert+ (/= z x))
=> id: 4
(assert+ (or w z))
=> id: 5
(check)
=> unsat
=> unsat core ids: 1 2 4
```

Assert (cont'd)

```
(define x::bool)
(define y::bool)
(assert (not x))
(assert (not y))
(assert+ (or x y))
=> 1
(check)
=> unsat
(retract 1)
(check)
=> sat
```

```
(define x::bool)
(define y::bool)
(assert (not x))
(assert (not y))
(assert+ (or x y));;id:1
(check)
(retract 1)
(check)
```

```
shyoon@shyoon-PC ~/yices-1.0.29-i686-p
$ ./yices assert.y
unsat
sat
```


Extracting models

`./yices -e exmodel.ys`

```
(define x::nat)
(define y::nat)
(assert (< x 3))
(assert (< y 3))
(assert (= x y))
(check)
```

```
shyoon@shyoon-PC ~/yices-
$ ./yices -e exmodel.ys
sat
(<= x 0)
(<= y 0)
```

- Finding another value set

```
(define x::nat)
(define y::nat)
(assert (< x 3))
(assert (< y 3))
(assert (= x y))
;;second
(assert (and (/= x 0) (/= y 0)))
(check)
```

```
shyoon@shyoon-PC ~/yices-
$ ./yices -e exmodel.ys
sat
(<= x 1)
(<= y 1)
```

Other value set

Conclusion

- Yices is an efficient and flexible SMT solver.
- Yices is freely available for end-users.
 - <http://yices.csl.sri.com/>
- Supported platform
 - Linux
 - Windows: cygwin & MinGW
 - Mac OSX
- Supported as a standalone tool and a library.
 - But, only GMT library(Linux).